# Contrasting Stabilities of Classical and Bridged Pyramidal $\mathrm{Si}_{3} \mathrm{H}_{3} \mathrm{X}$ Molecules ( $\mathrm{X}=\mathrm{BH}^{-}, \mathrm{CH}, \mathrm{N}, \mathrm{NH}^{+}, \mathrm{NO}, \mathrm{SiH}, \mathrm{P}, \mathrm{PH}^{+}$, and PO) 

Eluvathingal D. Jemmis* and Gantasala Naga Srinivas<br>Contribution from the School of Chemistry, University of Hyderabad, Hyderabad 500 046, India

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#### Abstract

Trigonal-pyramidal $\mathrm{Si}_{3} \mathrm{H}_{3} \mathrm{X}$ systems have been studied at HF/6-31G*, MP2(FC)/6-31G*, and Becke3LYP/ $6-31 \mathrm{G}^{*}$ levels. The classical trigonal-pyramidal structure (5) is a higher order stationary point for $\mathrm{X}=\mathrm{BH}^{-}, \mathrm{CH}$, $\mathrm{NO}, \mathrm{SiH}, \mathrm{P}, \mathrm{PH}^{+}$, and PO , whereas it is a minima for $\mathrm{X}=\mathrm{N}$ and $\mathrm{NH}^{+}$, at the MP2(FC)/6-31G* level. An alternative pyramidal structure ( $\mathbf{6}, C_{3 v}$ ) with three $\operatorname{SiHSi} 3 \mathrm{c}-2 \mathrm{e}$ bonds is minima, lower in energy than 5 by $47.7\left(\mathrm{X}=\mathrm{BH}^{-}\right)$, $39.1(\mathrm{X}=\mathrm{CH})$, $31.7(\mathrm{X}=\mathrm{N})$, $25.0\left(\mathrm{X}=\mathrm{NH}^{+}\right)$, $20.6(\mathrm{X}=\mathrm{SiH})$, $20.7(\mathrm{X}=\mathrm{P})$, $16.1\left(\mathrm{X}=\mathrm{PH}^{+}\right)$, and $18.2(\mathrm{X}=$ PO) $\mathrm{kcal} / \mathrm{mol}$. Isolobal analogy connects 6 with various triply hydrogen bridged pyramidal structures in organometallics.


## Introduction

There is a well-developed chemistry based on the smallest carbocyclic $\pi$-ligand $\eta^{3}-\mathrm{C}_{3} \mathrm{H}_{3}{ }^{+} .{ }^{1-3}$ Derivatives of $\mathbf{1}$ with main group and transition metal fragments (e.g. $\mathrm{C}_{4} \mathrm{R}_{4}\left(T_{d}\right)$ and $\mathrm{C}_{3} \mathrm{R}_{3}-$ $\left.\mathrm{Co}(\mathrm{CO})_{3}\right)$ are available in the literature. ${ }^{1,2}$ An all-boron analog of cyclopropenyl cation $\mathrm{B}_{3} \mathrm{H}_{6}{ }^{+}$is calculated to be a stable species. ${ }^{4}$ Theoretical studies on pyramidal structures ( $\mathbf{2}, C_{3 v}$ )

based on the $\mathrm{B}_{3} \mathrm{H}_{6}{ }^{+}$ligand have indicated them to be stable species on their potential energy surfaces. ${ }^{5}$ There are no reports on trigonal-pyramidal structures based on $\mathrm{Si}_{3} \mathrm{H}_{3}{ }^{+}$, the trisilacyclopropenyl cation, except for the studies on tetrasilatetrahedranes. ${ }^{6}$ The cation $\mathrm{Si}_{3} \mathrm{H}_{3}{ }^{+}$, found in the gas phase, is

[^0]calculated to be more stable as trisilacyclopropenium ion (3, $D_{3 h}$ ) with $2 \pi$ electron delocalization. ${ }^{7,8}$

An alternative triply hydrogen bridged structure $\left(\mathbf{4}, C_{3 v}\right)$ is also found to be a minimum for $\mathrm{Si}_{3} \mathrm{H}_{3}{ }^{+}$, but it is $42.0 \mathrm{kcal} / \mathrm{mol}$ higher in energy than $\mathbf{3}$ at the MP2(FC)/6-31G* level. ${ }^{8}$ There are reasons to believe that the $\mathrm{Si}_{3} \mathrm{H}_{3}$ ligand should be a more appropriate $\pi$-ligand than $\mathrm{C}_{3} \mathrm{H}_{3}$ on the basis of ring size. $\mathrm{C}_{5} \mathrm{H}_{5}$ is an ideal $\eta^{5}$ ligand in chemistry because of the ideal claw size of the $\pi$ framework of the $\mathrm{C}_{5} \mathrm{H}_{5}$ ring for a range of caps from main group and transition metal fragments. ${ }^{9}$ The cyclopropenyl cation provides a much smaller span of orbitals. This is compensated to an extent by the large out-of-plane bending of the ring substituents away from the capping group observed in $\mathrm{C}_{3} \mathrm{R}_{3}{ }^{+} \pi$-complexes. ${ }^{2}$ The longer SiSi bond length in $\mathrm{Si}_{3} \mathrm{H}_{3}{ }^{+}$ should reduce this orbital mismatch considerably. The bridged structure, 4, has an even longer SiSi distance. This brings in the interesting question of the relative stabilities of the classical structure 5 and the bridging structure 6. Structure $\mathbf{5}$ can be

considered as a homolog of $\mathbf{1}$, whereas structure $\mathbf{6}$ can be derived

[^1]Table 1. The Total Energies (au) and Zero-Point Energies (ZPE, kcal/mol) of Structures $\mathbf{5}$ and $\mathbf{6}$ for Various Caps at HF/6-31G*, MP2(FC)/ 6-31G*, and Becke3LYP/6-31G* Levels

| HF/6-31G* |  |  |  |  | MP2(FC)/6-31G* |  |  |  | Becke3LYP/6-31G* |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5 |  | 6 |  | 5 |  | 6 |  | 5 |  | 6 |  |
| cap | total energy | ZPE | total energy | ZPE | total energy | ZPE | total energy | ZPE | total energy | ZPE | total energy | ZPE |
| $\mathrm{BH}^{-}$ | -893.58893 | 22.8 | -893.65458 | 24.1 | -893.93912 | 21.2 | -894.01933 | 24.0 | -895.62773 | 20.7 | -895.70808 | 22.8 |
| CH | -906.75329 | 26.3 | -906.82467 | 27.4 | -907.14051 | 24.3 | -907.20677 | 26.9 | -908.83666 | 23.3 | -908.91038 | 25.8 |
| N | -922.78286 | 19.9 | -922.84882 | 19.2 | -923.21175 | 18.1 | -923.26361 | 19.0 | -924.91116 | 17.5 | -924.977621 | 18.0 |
| $\mathrm{NH}^{+}$ | -923.17848 | 28.0 | -923.22223 | 28.6 | -923.58258 | 25.7 | -923.62580 | 27.9 | -925.29129 | 25.1 | -925.34796 | 26.9 |
| NO | -997.51493 | 20.4 | -997.58465 | 21.0 |  |  | -998.17220 | 20.5 | -1000.04626 | 19.1 | -1000.07783 | 18.6 |
| SiH | -1157.82123 | 23.0 | -1157.84049 | 22.7 | -1158.14842 | 20.5 | -1158.18403 | 22.3 | -1160.23571 | 20.3 | -1160.28032 | 21.2 |
| P | -1209.10052 | 18.8 | -1209.12337 | 18.5 | -1209.45535 | 16.8 | -1209.49043 | 18.2 | -1211.54589 | 16.5 | -1211.59051 | 17.2 |
| $\mathrm{PH}^{+}$ | -1209.41746 | 23.5 | -1209.43578 | 23.5 | -1209.75711 | 21.5 | -1209.78535 | 23.2 | -1211.85828 | 20.8 | -1211.90181 | 22.0 |
| PO | -1283.89647 | 20.7 | -1283.92219 | 20.4 | -1284.43948 | 18.1 | -1284.47116 | 19.9 | -1286.71660 | 18.0 | -1286.76027 | 18.9 |

from 2 by replacing the BH group by Si using the isolobal analogy between BH and $\mathrm{Si}(7) .{ }^{10}$

The triply hydrogen bridged trigonal-pyramidal structures with metallacycles are known in the literature. For example, $\mathbf{6 b}\left(C_{3 v}\right)$ can be related to $(\mu-\mathrm{H})_{3} \mathrm{Fe}_{3}(\mathrm{CO})_{9}\left(\mu_{3}-\mathrm{CMe}\right)(\mathbf{8})$ through

isolobal analogy. ${ }^{11}$ We present here the results of a theoretical study on a series of pyramidal $\mathrm{Si}_{3} \mathrm{H}_{3}(\mathrm{X})$ compounds with $\mathrm{BH}^{-}$ $(5 \mathbf{a}, \mathbf{6 a}), \mathrm{CH}(5 \mathbf{b}, \mathbf{6 b}), \mathrm{N}(\mathbf{5 c}, \mathbf{6 c}), \mathrm{NH}^{+}(5 d, 6 d)$, $\mathrm{NO}(5 e, 6 e)$, $\mathrm{SiH}(\mathbf{5 f}, \mathbf{6 f}), \mathrm{P}(\mathbf{5 g}, \mathbf{6 g}), \mathrm{PH}^{+}(\mathbf{5 h}, \mathbf{6 h})$, and $\mathrm{PO}(\mathbf{5 i}, \mathbf{6 i})$ as capping groups ( X ) which support our contention that there is more flexibility for 4 in ring-cap bonding. H-bridged structures 6 are calculated to be more favorable than the classical, $\mathbf{5}$, in all cases.

## Method of Calculation

Geometries $\mathbf{5 a}-\mathbf{5 i}$ and $\mathbf{6 a}-\mathbf{6 i}$ were optimized under $C_{3 v}$ symmetry (except 5f, which has $T_{d}$ symmetry) at the HF/6-31G* level. ${ }^{12,13}$ The effect of electron correlation is obtained by further optimizing the structures at the MP2(FC)/6-31G* level. ${ }^{14}$ The density functional calculations at the Becke3LYP/6-31G* level were also done for comparison of relative energies. ${ }^{15}$ The nature of the stationary points was determined by analytical evaluation of the harmonic force constants and vibrational frequencies. ${ }^{16}$ All the calculations were carried out

[^2]Table 2. Relative Energies ${ }^{a}(\mathrm{kcal} / \mathrm{mol})$ of Structures 5 and 6 at HF/6-31G*, MP2(FC)/6-31G*, and Becke3LYP/6-31G* Levels (Values in Parentheses Are the Number of Imaginary Frequencies)

| HF/6-31G* |  |  | MP2(FC)/6-31G* |  | Becke3LYP/6-31G* |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cap | 5 | 6 | 5 | 6 | 5 | 6 |
| $\mathrm{BH}^{-}$ | 40.0(2) | 0.0(0) | 47.7(2) | 0.0(0) | 48.6(2) | 0.0(0) |
| CH | 43.8(0) | 0.0(0) | 39.1(2) | 0.0(0) | 44.0(2) | 0.0(0) |
| N | 42.0(0) | 0.0(0) | 31.7(0) | 0.0(0) | 41.3(0) | 0.0(0) |
| $\mathrm{NH}^{+}$ | 26.9(0) | 0.0(0) | 25.0(0) | 0.0(0) | 34.0(0) | 0.0(0) |
| NO | 43.2(2) | 0.0(0) | 67.3(0) ${ }^{\text {b }}$ | 0.0(0) | 20.3(2) | 0.0(0) |
| SiH | 12.4(0) | 0.0(0) | 20.6(2) | 0.0(0) | 27.2(0) | 0.0(0) |
| P | 14.6(0) | 0.0(0) | 20.7(2) | 0.0(0) | 27.4(0) | 0.0(0) |
| $\mathrm{PH}^{+}$ | 11.5(0) | 0.0(0) | 16.1(2) | 0.0(0) | 26.3(2) | 0.0(0) |
| PO | 16.4(0) | 0.0(0) | 18.2(2) | 0.0(0) | 26.6(0) | 0.0(0) |

${ }^{a}$ The relative energies are calculated after scaling the zero-point energy by 0.89 for HF/6-31G* and Becke3LYP/6-31G* levels and by 0.95 for the MP2(FC)/6-31G* level (ref 12). ${ }^{b}$ The structure corresponds to 9 (ref 37).
using the GAUSSIAN92 program package. ${ }^{17}$ The total and relative energies obtained from these calculations are given in Tables 1 and 2. Important geometrical parameters are listed in Tables 3 and 4. The MP2(FC)/6-31G* results are used in the discussion unless otherwise specified. These are qualitatively similar to those obtained at other levels.

## Results and Discussion

The H-bridged structure 6 is calculated to be lower in energy than the classical structure 5 at all three levels for all ring-cap combinations (Table 1). The stability of 6 over 5 ranges from $47.7 \mathrm{kcal} / \mathrm{mol}$ for X $=\mathrm{BH}^{-}$to $16.1 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{X}=\mathrm{PH}^{+}$. Similar trends are seen at the HF and Becke3LYP levels (Table 2). Structure 6 is found to be a minimum with all the caps. However, this is not true for the classical structure 5 , which is a higher order saddle point for $\mathrm{BH}^{-}, \mathrm{CH}, \mathrm{SiH}, \mathrm{P}$, $\mathrm{PH}^{+}$, and PO caps. Structure 5 is calculated to be a minimum for $\mathrm{NH}^{+}$ and N . The caps $\mathrm{BH}^{-}, \mathrm{CH}$, and $\mathrm{PH}^{+}$followed the same trend at the Becke3LYP level, whereas structures with $\mathrm{SiH}, \mathrm{P}$, and PO caps are shown to be minimum at this level. The classical structure with NO cap (5e) collapses to $\mathbf{9}\left(C_{3 v}\right)$ on optimization at the MP2(FC) level. On the other hand the triply hydrogen bridged structure $\mathbf{6 e}$ is a minimum. The classical structure 5f, with SiH cap (one of the nine caps considered in the present study), is tetrasilatetrahedrane. Previous calculations on $\mathrm{Si}_{4} \mathrm{H}_{4}$ have shown that the tetrasilatetrahedrane is a local minimum at the HF/6-31G* level on the potential energy surface of $\mathrm{Si}_{4} \mathrm{H}_{4}{ }^{6}{ }^{6}$ However, Nagase et al. predicted that two SiSi bonds in $\mathbf{5 f}$ can be broken without a barrier to form a four-membered ring isomer at higher levels. ${ }^{18}$ In the present study the tetrasilatetrahedrane is found to be a

[^3]Table 3. Important Geometrical Parameters for $\mathrm{Si}_{3} \mathrm{H}_{3} \mathrm{X}(5)$ at HF/6-31G*, MP2(FC)/6-31G*, and Becke3LYP/6-31G* Levels ${ }^{a}$

| HF/6-31G* |  |  |  |  | MP2(FC)/6-31G* |  |  |  | Becke3LYP/6-31G* |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cap | X -Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{1}{ }^{\text {b }}$ | X-Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{1}{ }^{\text {b }}$ | X-Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{1}{ }^{\text {b }}$ |
| $\mathrm{BH}^{-}$ | 2.072 | 2.285 | 1.479 | 20.4 | 2.051 | 2.289 | 1.491 | 21.1 | 2.078 | 2.298 | 1.494 | 22.7 |
| CH | 1.900 | 2.257 | 1.465 | -7.8 | 1.904 | 2.337 | 1.489 | -31.7 | 1.908 | 2.430 | 1.504 | -41.2 |
| N | 1.808 | 2.238 | 1.467 | -18.0 | 1.861 | 2.286 | 1.486 | -29.5 | 1.843 | 2.308 | 1.492 | -30.9 |
| $\mathrm{NH}^{+}$ | 1.869 | 2.249 | 1.458 | -15.5 | 1.886 | 2.298 | 1.477 | -23.7 | 1.887 | 2.308 | 1.482 | -25.0 |
| NO | 1.824 | 2.267 | 1.462 | -18.0 |  |  |  |  | 1.975 | 2.484 | 1.500 | -49.9 |
| SiH | 2.314 | 2.314 | 1.464 | 19.5 | 2.315 | 2.315 | 1.478 | 19.5 | 2.327 | 2.327 | 1.479 | 19.5 |
| P | 2.292 | 2.247 | 1.463 | 4.4 | 2.304 | 2.256 | 1.479 | -2.6 | 2.325 | 2.266 | 1.481 | -0.6 |
| $\mathrm{PH}^{+}$ | 2.266 | 2.301 | 1.457 | 2.9 | 2.265 | 2.318 | 1.475 | -2.3 | 2.284 | 2.332 | 1.477 | -2.8 |
| PO | 2.247 | 2.319 | 1.462 | 15.8 | 2.272 | 2.333 | 1.478 | 18.6 | 2.287 | 2.343 | 1.499 | 18.4 |

[^4] indicates that the hydrogens are bent away from the cap (X).

Table 4. Important Geometrical Parameters for $\mathrm{Si}_{3} \mathrm{H}_{3} \mathrm{X}$ (6) at HF/6-31G*, MP2(FC)/6-31G*, and Becke3LYP/6-31G* Levels ${ }^{a}$

| HF/6-31G* |  |  |  |  | MP2(FC)/6-31G* |  |  |  | Becke3LYP/6-31G* |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cap | X-Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{2}{ }^{\text {b }}$ | X-Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{2}{ }^{\text {b }}$ | X-Si | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{Si}-\mathrm{H}$ | $\theta_{2}{ }^{\text {b }}$ |
| $\mathrm{BH}^{-}$ | 2.008 | 2.618 | 1.714 | 35.2 | 1.988 | 2.558 | 1.715 | 35.1 | 2.006 | 2.614 | 1.731 | 35.5 |
| CH | 1.885 | 2.629 | 1.700 | 33.9 | 1.884 | 2.595 | 1.698 | 33.3 | 1.897 | 2.635 | 1.714 | 33.5 |
| N | 1.793 | 2.563 | 1.714 | 35.0 | 1.829 | 2.534 | 1.706 | 34.7 | 1.825 | 2.565 | 1.725 | 34.7 |
| $\mathrm{NH}^{+}$ | 1.871 | 2.695 | 1.683 | 31.8 | 1.879 | 2.678 | 1.684 | 30.9 | 1.889 | 2.712 | 1.699 | 30.9 |
| NO | 1.807 | 2.644 | 1.715 | 33.3 | 1.838 | 2.626 | 1.706 | 32.4 | 1.878 | 2.654 | 1.713 | 32.9 |
| SiH | 2.317 | 2.833 | 1.695 | 29.6 | 2.283 | 2.715 | 1.695 | 30.0 | 2.316 | 2.822 | 1.711 | 30.0 |
| P | 2.265 | 2.694 | 1.684 | 32.2 | 2.257 | 2.619 | 1.686 | 32.1 | 2.286 | 2.696 | 1.702 | 32.1 |
| $\mathrm{PH}^{+}$ | 2.276 | 2.926 | 1.697 | 27.5 | 2.245 | 2.842 | 1.695 | 27.2 | 2.283 | 2.923 | 1.712 | 27.3 |
| PO | 2.245 | 2.827 | 1.694 | 29.6 | 2.230 | 2.721 | 1.692 | 29.5 | 2.271 | 2.821 | 1.709 | 29.7 |

${ }^{a}$ Distances are in angstroms and angles are in degrees. ${ }^{b} \theta_{2}$ represents the angle between the $\mathrm{Si}_{3}$ plane and SiHSi plane.
second-order saddle point at the MP2(FC) level. The two imaginary frequencies are found to follow the path suggested by Nagase et al. to break the two SiSi bonds. However, $\mathbf{5 f}$ is calculated to be a minimum at the Becke3LYP level supporting the HF level of calculations. It was also indicated that silyl substitution can stabilize 5f. ${ }^{19}$ The tetrasilatetrahedrane $\left(\mathrm{Si}_{4} \mathrm{R}_{4}\right)$ has been synthesized with a "super silyl" group $\left(\mathrm{R}=t\right.$ - $\mathrm{Bu} \mathrm{u}_{3} \mathrm{Si}$ ). ${ }^{20}$ The $C_{3 v}$ isomer of $\mathrm{Si}_{4} \mathrm{H}_{4}, \mathbf{6 f}$, is calculated to be $20.6 \mathrm{kcal} / \mathrm{mol}(12.4$ and $27.2 \mathrm{kcal} / \mathrm{mol}$ at the HF and Becke3LYP levels, respectively) more stable than the $T_{d}$ arrangement, $\mathbf{5 f}$. But $\mathbf{6 f}$ is $28.7 \mathrm{kcal} / \mathrm{mol}$ higher in energy than the lowest energy isomer ( $\mathbf{1 0}$, $C_{s}$ ), reported in the literature for $\mathrm{Si}_{4} \mathrm{H}_{4} .^{6 e, 21}$ The tetrahedral structure observed for $\mathrm{Si}_{4} \mathrm{R}_{4}$ experimentally points to the effect of substituents in controlling the structures; the propensity for bridging does not seem to go beyond hydrogens.


The SiSi distances (Table 3) in the classical structure 5 are in the range of single bonds $\left(2.332 \AA\right.$ in trisilacyclopropane $\left(\mathbf{1 1}, D_{3 h}\right)$ and $2.334 \AA$ in disilane). ${ }^{22-24}$ The bridged structure 6 has considerably

[^5]shortened SiSi distances (Table 4) compared to the triply hydrogen bridged trisilacyclopropane $\left(\mathbf{1 2}, C_{3 v}\right), \mathrm{Si}_{3} \mathrm{H}_{6}(3.080 \AA) .{ }^{23}$


11


12


NBO analysis shows the bonding in $\mathbf{5}$ to be classical. ${ }^{25}$ The triply hydrogen bridged structure $\mathbf{6}$ has three each of $2 \mathrm{c}-2 \mathrm{e}$ XSi bonds, the SiHSi $3 \mathrm{c}-2 \mathrm{e}$ bond, and lone pairs on the silicon atom of the $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring. The geometrical constraints in 5 force bent bonds between the cap (X) and $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring (13). The deviation of the XSi bonds from the internuclear axis $\left(\theta_{3}\right)$ at X in $\mathbf{5}$ and $\mathbf{6}$ obtained from the NBO analysis is listed in Table 5. $\theta_{3}$ is smaller in 6 compare to 5 . That is the XSi bond becomes more directed in $\mathbf{6}$ leading to better bonding. The NBO analysis also reveals that the lone pair on divalent Si in 6 is predominantly of s character ( $\sim 73 \%$ ). This leaves maximum pcharacter for XSi bonds $(\sim 86 \%)$. Since the lone pair on Si has greater s character, it looses the directionality and is in the plane of the $\mathrm{Si}_{3}$ ring rather than in the anticipated direction, away from the cap. Thus the coplanarity of lone pairs on the $\mathrm{Si}_{3}$ ring pushes the $\mathrm{p}_{\pi}$ orbital toward X , resulting in better overlap between X and the $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring. ${ }^{26}$ This type of arrangement is absent in $\mathbf{5}$, leading to poor overlap between $X$ and the $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring. The Mulliken overlap population between X and Si increases in going from 5 to $\mathbf{6}$ for all $\mathrm{X}\left(0.210,0.388\right.$ for $\mathrm{BH}^{-}$;

[^6]Table 5. The Bond Bending Angle ( $\theta_{3}$, the Deviation of Hybrid Orbital from the XSi Axis) (in deg) at X at the HF/6-31G*// MP2(FC)/6-31G* Level from NBO Analysis

| cap | $\theta_{3}(\mathbf{5})$ | $\theta_{3}(\mathbf{6})$ |
| :--- | :---: | :---: |
| $\mathrm{BH}^{-}$ | 29.7 | 22.8 |
| CH | 25.7 | 18.3 |
| N | 19.6 | 14.5 |
| $\mathrm{NH}^{+}$ | 25.5 | 15.3 |
| NO |  | 14.5 |
| SiH | 32.6 | 25.4 |
| P | 25.1 | 18.8 |
| $\mathrm{PH}^{+}$ | 32.6 | 23.0 |
| PO | 32.0 | 23.9 |

0.206, 0.309 for $\mathrm{CH} ; 0.180,0.253$ for $\mathrm{N} ; 0.053,0.144$ for $\mathrm{NH}^{+} ;-0.001$, 0.271 for $\mathrm{SiH} ; 0.132,0.248$ for $\mathrm{P} ;-0.019,0.178$ for $\mathrm{PH}^{+}$; and 0.011 , 0.240 for PO ). These changes in overlap population also indicate the better bonding between X and $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring in $\mathbf{6}$ compared to 5 .

The bonding in 5 and $\mathbf{6}$ can also be explained by the six interstitial electron rule for three-dimensional delocalization in pyramidal systems. ${ }^{3}$ According to this rule, the $\mathrm{Si}_{3} \mathrm{H}_{3}$ ring provides $3 \pi$ electrons and the cap, $X$, provides three electrons leading to a total of six electrons to fill the three bonding combinations obtained from the ring and cap orbitals. All X groups considered here are selected on the basis of this interstitial electron rule. The caps $\mathrm{BH}^{-}, \mathrm{CH}, \mathrm{N}$, and $\mathrm{NH}^{+}$are selected from the previous theoretical calculations on carbocyclic pyramidal structures. ${ }^{3} \mathrm{P}, \mathrm{PH}^{+}$, and SiH are selected to see the effect of heavier analogs. The report on interaction between CO and cyclobutadiene ${ }^{27}$ suggested the possibility of nitrosyl (NO) and phosphoryl (PO) groups as caps in the present study. The bonding with these caps ( NO and PO ) is due to the degenerate $\pi$-orbitals of $\mathrm{Si}_{3} \mathrm{H}_{3}$ and the degenerate $\pi^{*}$-orbitals of NO and PO. Therefore, the $\mathrm{N}-\mathrm{O}$ (6e: $1.396 \AA$ ) and $\mathrm{P}-\mathrm{O}(\mathbf{5 i}: 1.512 \AA, 6 \mathrm{i}: 1.517 \AA$ ) distances in $\mathbf{5}$ and 6 are close to their respective single bond distances. ${ }^{28}$ The changes in $\mathrm{B}-\mathrm{H}, \mathrm{C}-\mathrm{H}, \mathrm{N}-\mathrm{H}, \mathrm{Si}-\mathrm{H}$ (cap), and $\mathrm{P}-\mathrm{O}$ bond lengths are found to be minimal between structures 5 and 6. ${ }^{29}$ The negative $\theta_{1}$ (bending of terminal $\mathrm{Si}-\mathrm{H}$ bonds toward the cap) in $\mathbf{5 b}, \mathbf{5 c}, \mathbf{5 d}, \mathbf{5 g}$, and $\mathbf{5 h}$ (Table 3) can be explained by the concept of the compatibility of orbitals in overlap. ${ }^{3}$ The relatively less diffuse $\mathrm{p}_{\pi}$-orbital on the cap $(\mathrm{X})$ pushes the $\mathrm{H}_{\mathrm{t}}$ toward the cap for better interaction.

Structure 6 is related to the triply hydrogen bridged isomer of $\mathrm{Si}_{3} \mathrm{H}_{6}$ (12). ${ }^{23}$ Bridged structure $\mathbf{1 2}$ is calculated to be $84.0 \mathrm{kcal} / \mathrm{mol}$ higher in energy than the classical structure 11. Since the three terminal hydrogens are directed toward a converging point along $\mathrm{SiH}_{\mathrm{t}}$ axes in 12, these hydrogens can be replaced by a 3-electron donor cap (X) (similar to the replacement of nonbonded hydrogen repulsions in [10]annulene by a $\mathrm{CH}_{2}$ bridge ${ }^{30}$ ) leading to structure 6. In contrast, the classical structure of $\mathrm{Si}_{3} \mathrm{H}_{6}$ (11) has divergent hydrogens. The advantage in the formation of the pyramidal molecules with capping X provided by the SiH bond directions in $\mathbf{1 2}$ in comparison to those in $\mathbf{1 1}$ is reflected in the uniformly lower energy of $\mathbf{6}$.

Similarly the "isosynaptic analogy" connects the structural patterns in silicon chemistry with organometallic chemistry. ${ }^{31}$ Thus using this analogy, we can equate $(\mu-\mathrm{H})_{3} \mathrm{Fe}_{3}(\mathrm{CO})_{9}\left(\mu_{3}-\mathrm{CMe}\right),{ }^{11}(\mu-\mathrm{H})_{3} \mathrm{Os}_{3}(\mathrm{CO})_{9}-$ $\left(\mu_{3}-\mathrm{CX}\right)\left(\mathrm{X}=\mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}, \mathrm{Cl}\right),{ }^{32}(\mu-\mathrm{H})_{3} \mathrm{Co}_{3} \mathrm{Cp}^{*}\left(\mu_{3}-\mathrm{CMe}\right),{ }^{33}$ and $(\mu-\mathrm{H})_{3}-$

[^7]Table 6. Energy of the Reaction $\left(\Delta E_{1}\right)$ for Eq 1 and $\Delta E_{2}$ for Eq 2 at the MP2(FC)/6-31G* Level

| cap | $\Delta E_{1}(\mathrm{kcal} / \mathrm{mol})$ | $\Delta E_{2}(\mathrm{kcal} / \mathrm{mol})$ |
| :--- | :---: | :---: |
| $\mathrm{BH}^{-}$ | -89.7 | -129.5 |
| CH | -81.1 | -120.9 |
| N | -73.7 | -113.5 |
| $\mathrm{NH}^{+}$ | -67.1 | -106.8 |
| SiH | -62.7 | -102.5 |
| P | -62.7 | -102.5 |
| $\mathrm{PH}^{+}$ | -58.1 | -97.9 |
| PO | -60.2 | -100.0 |

$\mathrm{Os}_{3}(\mathrm{CO})_{9}\left(\mu_{3}-\mathrm{CBCl}_{2}\right)^{34}$ with $\mathbf{6 b}$ and $(\mu-\mathrm{H})_{3} \mathrm{Os}_{3}(\mathrm{CO})_{9}\left(\mu_{3}-\mathrm{BCO}\right)^{35}$ with $\mathbf{6 a}$.
The low relative energies of $\mathbf{5}$ and $\mathbf{6}$ hide the enormous advantage of the triply bridging 4 in interacting with $X^{-}$. Even though 4 is less stable than 3, $\mathbf{6}$ obtained by complexing $\mathbf{4}$ and $\mathrm{X}^{-}$is more favorable than 5 (eq 1, Table 6). The strain energies involved in going from 12

to $\mathbf{6}$ and from $\mathbf{1 1}$ to 5 are not the same. An estimate of their difference is obtained from eq 2. The high exothermicity of this equation is also

a reflection of the increased strain in $\mathbf{5}$ in relation to $\mathbf{6}$. Thus the classical trigonal-pyramidal structure (5) is found to be relatively more strained compared to the triply hydrogen bridged structure $\mathbf{6}$. The $\mathrm{X}-\mathrm{Si}_{3} \mathrm{H}_{3}$ binding is more favorable in $\mathbf{6}$. In fact structure $\mathbf{6}$ is more favorable than 5, not only for $\mathrm{Si}_{4} \mathrm{H}_{4}$ but also for $\mathrm{Ge}_{4} \mathrm{H}_{4}$. The triply H -bridged $\mathrm{Ge}_{4} \mathrm{H}_{4}$ is calculated to be $57.6 \mathrm{kcal} / \mathrm{mol}$ more stable than the classical structure at the Becke3LYP/LANL1DZ level. ${ }^{36}$ The classical tetrahedrane structure is a higher order saddle point for $\mathrm{Ge}_{4} \mathrm{H}_{4}$.

[^8]Other heavier analogs are expected to follow this trend. Therefore the pyramidal compounds (6) should be attractive synthetic targets.

## Conclusions

Calculations at the HF/6-31G*, MP2(FC)/6-31G* and Becke3LYP/6-31G* levels show the following: The classical pyramidal structure is a second-order stationary point for all 5 except for $\mathrm{X}=\mathrm{N}$ and $\mathrm{NH}^{+}$at the MP2(FC) level. The $C_{3 v}$ alternatives (6) are minima and lower in energy than 5. Structure 6 is related to $\mathrm{B}_{3} \mathrm{H}_{6} \mathrm{X}$ through isolobal analogy and
(36) (a) The basis set LANL1DZ uses the Dunning-Huzinaga valence double- $\zeta$ on hydrogen and Los Alamos effective core potentials plus double- $\zeta$ on Ge: Hay, P. J.; Wadt, W. R. J. Chem. Phys. 1985, 82, 270, 299. Wadt, W. R.; Hay, P. J. J. Chem. Phys. 1985, 82, 284. (b) The total energy for triply hydrogen bridged $C_{3 v}$ structure of $\mathrm{Ge}_{4} \mathrm{H}_{4}$ is -17.42525 au at the Becke3LYP/LANL1DZ level.
(37) The MP2(FC)/6-31G* energy for structure 9 is -998.16338 au and the zero-point energy is $85.5 \mathrm{kcal} / \mathrm{mol}$.
to triply hydrogen bridged pyramidal structures in organometallics through isosynaptic analogy. The isodesmic equation between $\mathrm{X}^{-}$and $\mathrm{Si}_{3} \mathrm{H}_{3}{ }^{+}$has shown that ring-cap interaction in $\mathbf{6}$ is better than that in 5 . Similarly, eq 2 shows that $\mathbf{6}$ is relatively less strained than 5.

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